

1.1 $P = f \{ C, Y, T \}$ where C, Y, and T are variables endogenous to the security

P = Market Price

C = Cash Receipts, periodic coupon, dividend or premium payments

Y = Yield, a single term relating security's return, relative to P, C, T

T = Time, a terminal or continuous measure of the life of the security.

Figure 2

1.2 Yield
$$M = \sum (Maturity \times Portfolio Coefficient \times YTM)$$
, for all issues $\sum (Maturity \times Portfolio Coefficient)$, for all issues

where Yield M = Governing Yield = Y

Maturity = Time = Maturity in Years

Portfolio Coefficient = Present Value, per issue/Present Value, ∑ issues

Present Value = Accrued Interest + (best bid Price × Face Value)

YTM = Yield-To-Maturity, a means providing yield respective time.

Figure 3

1.2d Yield Md =
$$\frac{\sum (Duration \times Portfolio Coefficient \times YTM), for all issues}{\sum (Duration \times Portfolio Coefficient), for all issues}$$

Figure 4

(Duration, modified annualized)
$$1.3 K = \frac{-C}{Y^2} (1 - (1 + Y/2)^{-2T}) + \frac{C}{Y} (T + TY/2)^{-2T-1} - (T + TY/2)^{-2T-1}$$

1.3w K =
$$\frac{-C}{Y^2} + \frac{C}{Y^2} (1 + Y/2)^{-2T} - (1 - C/Y)(T + TY/2)^{-2T-1}$$

Figure 5

(Convexity)
$$\frac{2C}{Y^3} - \frac{CT}{(1+Y/2)^{2T}} - \frac{CT}{Y^2} - \frac{C}{(1+Y/2)^{2T+1}} - \frac{C}{(T+TY/2)^{2T+1}} + \frac{(1+C/Y)(T^2+T/2)}{(T+TY/2)^{2T+2}}$$

Figure 6

- 1.5 Portfolio Coefficient, for each Issue = Present Value Present Value;
- where 1.5a Present Value^I = (AI + (Bid Price × Face Value)), for each Issue;
- 1.5b Present Value^P = \sum (AI + (Bid Price × Face Value)), for all Issues.

- 1.6a Present Value^P = \sum (AI + (Bid Price × Face Value), for all Issues;
- 1.6b Accrued Interest $^{P} = \sum$ Accrued Interest, AI, for all Issues;
- 1.6c Face Value^P = \sum Face Value, for all Issues:
- 1.6d Implied Price P = (Present Value P AI P)/ Σ Face Value, for all Issues.

Figure 8

- 1.7a $C^P = Cash Flow^P = \sum C \times Portfolio Coefficient, for all Issues;$
- 1.7b $T^P = Time^P = \sum Maturity \times Portfolio Coefficient, for all Issues;$
- 1.7c $Y^P = Yield^P = \sum Yield \times Portfolio Coefficient, for all Issues.$

Figure 9

- 1.8a $C^P = Coupon^P = \sum Coupon \times Portfolio Coefficient, for all Issues;$
- 1.8b $T^P = Maturity^P = \sum Maturity \times Portfolio Coefficient, for all Issues;$
- 1.8c $Y^P = Yield^P = \sum Yield \times Portfolio Coefficient, for all Issues.$

Figure 10

- 1.9a Duration^P = \sum Duration × Portfolio Coefficient, for all Issues;
- 1.9b Convexity^P = \sum Convexity × Portfolio Coefficient, for all Issues.

Figure 14

Portfolio Coefficient, for each Issue = Present Value¹/Present Value¹;

Present Value¹ = (AI + (Bid Price x Face Value), for each Issue;

Present Value² = Σ (AI+(Bid Price x Face Value), for all Issues

Face Value³ = Σ Face Value, for all Issues;

Present (Full) $Value^{P} = \Sigma$ (AI + (Bid Price x Face Value), for all Issues; Accrued Interest^P = Σ Accrued Interest, AI, for all Issues;

Implied Price^P = (Present Value^P – AI^P)/ Σ Face Value for all Issues

 $C^{P} = Cash Flow^{P} = \sum C \times Portfolio Coefficient, for all Issues;$

 $T^P = Time^P = \Sigma$ Maturity x Portfolio Coefficient, for all Issues;

 $Y^{p} = Yield^{p} = \Sigma Yield \times Portfolio Coefficient, for all Issues$

Duration^P = Σ Duration x Portfolio Coefficient, for all Issues; Convexity^P = Σ Convexity x Portfolio Coefficient, for all Issues

Figure 15

Aggregate Data Values for Portfolio							
Date	3/22/96	4/3/96	4/25/96				
Face Value ^P	\$510,000,000	\$510,000,000	\$510,000,000				
Accrued Interest ^P	\$4,749,907	\$5,387,107	\$7,172,578				
Present Value ^P	\$513,449,907	\$513,848,982	\$513,610,078				
Implied Price ^P	0.99745098	0.99698407	0.99301471				
Portfolio Coefficient							
11/96	.1375888	.1377205	.138186				
5/97	.1959174	.1961886	.196814				
10/97	.0799234	.0798135	.196814				
8/98	.2353559	.235331	.235427				
3/99	.0779432	.077984	.077894				
6/00	.1572929	.157415	.156749				
2/01	.1159784	.115547	.114773				
Coupon ^P	5.680331%	5.680322%	5.667059%				
Maturity ^P	2.470660	2.437096	2.359601				
YTM ^P	5.730002%	5.755183%	5.859601%				
Duration ^P	2.222031	2.191867	2.130696				
Convexity ^P	7.847886	7.695562	7.389558				

Figure 20

Convexity, V vs. Prior Art			
Date	3/22/96	4/3/96	4/25/96
P			
Yield M ^P	5.87129004%	5.89269332%	6.0661141%
YTM ^P	5.73000157%	5.75518286%	5.8561971%
Yield M ^P – YTM ^P (bp spread)	0.14128852	0.13751046	0.2099176
Coupon ^P	5.680330985%	5.680322119%	5.66705895%
Maturity P	2.4706604	2.437096	2.359601
Price ^P (N/A for V)	99.745098	99.698407	99.301471
process determining Convexi	ty, using above sing	le aggregate C ^P , Y ^P , T ^P	values:
V (1.4c, Yield M ^P)	6.41019700	6.25535943	5.88053355
$V (1.4c, YTM^P)$	6.44053175	6.28389014	5.92058762
V (1.4cv, Yield $M_{}^{P}$ – YTM P)	6.84893917	7.14436415	2.89621154
V (1.4cv, Yield M ^P)	0.00404544	0.00396111	0.00360859
Prior Art (S.4, YTM ^P)	6.05221587	5.91149933	5.60084222
	•		
Market Spot Yield	5.845%	5.875%	6.065%
Yield M – Zero Spot	0.026%	0.018%	0.001%

Figure 21

Period	3/22/96 - 4/3/96	4/3/96 - 4/25/96	3/22/96 - 4/25/96
δΥ	0.0002071580	0.0017921768	0.001968276
K	-2.25389446	-2.21483844	-2.25389446
V (1.4cv, b.p. spread)	6.84893917	7.14436415	6.84893917
V (1.4c, Yield M)	6.41019700	6.25535943	6.41019700
V (1.4cv, Yield M)	0.00404544	0.00396111	0.00404544
processing 1.10, estimated Δ	Price = $(K \times \delta Y)$	$+ (0.5 \times V \times (\delta Y)^2)$:	
Actual Δ Price	-0.000466911	-0.003969363	-0.004436274
Est. Δ P (V=1.4cv, spread)	-0.000466766	-0.003957909	-0.004423097
Accuracy %	99.97%	99.71%	99.70%
Error %	0.03%	0.29%	0.30%
Est. $\Delta P (V=1.4c \text{ YieldM}^P)$	-0.000466775	-0.003959336	-0.004423869
Accuracy %	99.97%	99.75%	99.72%
Error %	0.03%	0.25%	0.28%

Figure 26A

```
1.2 Yield M =YM = (sum{(Maturity*Portfolio Coefficient*YTM)<sub>1</sub>, (M*PC*YTM)<sub>2</sub>,...})/
(sum{(Maturity*Portfolio Coefficient)<sub>1</sub>, (M*PC)<sub>2</sub>,...})

1.2d Yield Md =YMD = (sum{(Duration*PC*YTM)<sub>1</sub>, (D*PC*YTM)<sub>2</sub>,...})/
(sum{(Duration*Portfolio Coefficient)<sub>1</sub>, (D*PC)<sub>2</sub>,...})
```

Figure 26B

```
1.3cw K = DPDY = ((-C/(Y^2))^*(1-((1+(.5*Y))^*(-2*T))))

semi-annual +((C/Y)^*((T+(.5*Y*T))^*((-2*T)-1)))

-((T+(.5*Y*T))^*((-2*T)-1)))

where C and Y are decimal values, T=Maturity in years

1.3cn K =BONK= ((-C/(Y^2))^*(1-((1+(Y/N))^*(-N*T))))

generalized +(((C/Y)-1)^*T^*((1+(Y/N))^*((-N*T)-1)))

where N=n= # cash receipts per annum, e.g. semi-annual=2; T=Maturity in years and where BONK and DPDY not returning exact identical values for N=n=2
```

Figure 26C

```
1.4cn
        V
              =BONV=
                           (((2*C)/(Y^3))*(1-(Y/N))^(-N*T)))
generalized
                           -((C/Y^2)*(2*T)*((1+(Y/N))^((-N*T)-1)))
                           -(((C/Y)-1)*(((N*T)+1)*(T/N))*((1+(Y/N))^{((-N*T)-2)))
       where N=n=# cash receipts per annum, e.g. semi-annual=2; T=Maturity in years
1.4cv
        V
             =VEXA=
                           (((2*C)/(Y^3)) - (((2*C)/(Y^3))*((1+(Y/2))^(-2*T)))
spread-based, semi-annual
                           -((C*T)/(Y^2))*((1+(Y/2))^((-2*T)-1))
                           -((C/(Y^2))*((T+(T*(Y/2)))^((-2*T)-1)))
                    +((1+(C/Y))*((T^2)+(T/2))*((T+(T*(Y/2)))^((-2*T)-2)))/10000
              where e.g. Y=YieldM-YTM, Y expressed in decimal, i.e. if Y=0.14%=0.14
1.4cvn V
             =VEX=
                           (((2*C)/(Y^3)) - (((2*C)/(Y^3))*((1+(Y/N))^(-N*T)))
spread-based, generalized
                           -((C*T)/(Y^2))*((1+(Y/N))^((-N*T)-1))
                           -((C/(Y^2))*((T+(T*(Y/N)))^((-N*T)-1)))
                    +((1+(C/Y))*((T^2)+(T/N))*((T+(T*(Y/N)))^((-N*T)-2)))/10000
              where e.g. Y = Yield M, Y = expressed in decimal, i.e. if Y = 6.06\% = 0.606
```

Figure 26D

```
1.10c generalized \Delta P = DELTAP = K*(CHY) + (0.5*V*(CHY^2))
and where \Delta P = DELTAP = -abs(Duration1.3n)*(CHY)+(0.5*(Convexity1.4cvn)*(CHY^2))
```

Figure 26E

1.11 universal $\Delta P = DP = -abs(Duration)*(CHY)+(0.5*(Convexity)*(CHY^2))$	
---	--

Figure 39

Target Security, a U.S. Treasury Note, he	eld to mature 5/15/99, as on April 3, 1996:
Maturity:	May 1999
Coupon:	6.75% per annum, semi-annual payments
Prices: Bid/Ask	102:07; 102:07 / 102:09; 102:11
Face Value:	\$50 million
Best Price:	\$51,140,625
Accrued Interest:	\$1,300,205
Total Cost (P+AI):	\$52,440,830
Duration (mod. ann.):	2.782972

Figure 40

Target	of Duration 2.7829	can be sold for \$52,409,580	and bought for \$52,440,830
REPS A	2.6104	can be sold for \$52,383,749	and bought for \$52,416,144
REPS B	2.8280	can be sold for \$52,450,920	and bought for \$52,450,977
REPS C	2.6038	can be sold for \$52,351,321	and bought for \$52,383,845

Figure 41

	Arbitrage	Opportunities		Sorted Arbitrage Opportunities			
Buying	Selling	\$ Arb. Differ.	Spread bp	Buying	Selling	\$ Arb. Diff.	Spread bp
Target	Α	-31250	-0.0006	c	В	67075	0.00128
Target	В	-57081	-0.00109	A	В	34776	0.000663
Target	С	-89509	-0.00171	C	Target	25735	0.000491
Α	Target	-6564	-0.00013	c	Α	-96	-1.8E-06
Α	В	34776	0.000663	A	Target	-6564	-0.00013
Α	С	-64823	-0.00124	Target	Α	-31250	-0.0006
В	Target	-41397	-0.00079	В	Target	-41397	-0.00079
В	Α	-67228	-0.00128	Target	В	-57081	-0.00109
В	С	-99656	-0.0019	A	С	-64823	-0.00124
С	Target	25735	0.000491	В	Α	-67228	-0.00128
С	Α	-96	-1.8E-06	Target	С	-89509	-0.00171
С	В	67075	0.00128	В	С	-99656	-0.0019

Figure 47

Scalar			Nominal \$	Values				Adj \$ 1972	Values	
Value \$	Annual	Actual \$B	Actual \$B	Actual \$B	Actual \$B	Annual				Adj \$B
	Year End		Catastroph	Net Depos	Statutory L	Year End	Adj\$ 1972	Adj1972 \$E	Adj\$1972	Stat Loss
CPI	Year End	FDIC	Loss,PCS	Loss	P/C Under	Year End	DepCI	CatLoss	DepLoss	Underwr
0.26699	12/31/96		7.35			12/31/96		1.962379		
0.275		0.632		0.332	14.2	12/31/95		2.292125	0.0913	3.905
0.2875 0.2875		1.236		0.636	19	12/31/94		4.900438		
0.2075		3.132 40.94	5.585 22.974	2.132 32.34		12/31/93		1.605688	0.61295	
0.3125		53.832	4.711	39.732	33.3 16.7	12/31/92 12/31/91		6.8922 1.472188	9.702	
0.325		14.489	2.807	6.889	18.2			0.912275		5.21875 5.915
0.3375	12/31/89	22.28	7.642	17.58	16.5	12/31/89		2.579175	5.93325	5.56875
0.35	12/31/88	36.432	1.409	32.132	8.4	12/31/88	12.7512		11.2462	
0.3625	12/31/87	8.4	0.946	5.4	7.1	12/31/87		0.342925	1.9575	2.57375
0.375		7.057	0.871	4.057	13.7	12/31/86	2.646375	0.326625	1.521375	5.1375
0.3875		8.059	2.816	6.359	22.6		3.122863			8.7575
0.4	12/31/84	20.334	1.548	14.834	19.4	12/31/84	8.1336		5.9336	7.76
0.425 0.4375	12/31/83 12/31/82	5.442 9.904	2.255 1.523	3.242 9.104		12/31/83		0.958375	1.37785	4.7175
0.4625	12/31/82	3.826	0.714	3.756	8.3 4.5	12/31/82 12/31/81		0.666313 0.330225	3.983	3.63125
0.5125	12/31/80	5.516	1.178	5.416	1.7	12/31/81		0.330225	1.73715 2.7757	2.08125 0.87125
0.575	12/31/79	0.111	1.705	3.410	-0.02			0.980375	2.7737	-0.0115
0.6375	12/31/78	0.854	0.645		-2.5			0.411188		-1.59375
0.6875	12/31/77	0.205	0.423		-1.9			0.290813		-1.30625
0.7375	12/31/76	1.235	0.271		1.6			0.199863		1.18
0.775	12/31/75	0.34	0.513		3.6	12/31/75		0.397575		2.79
0.85	12/31/74	1.576	0.696		1.9	12/31/74	1.3396	0.5916		1.615
0.9375	12/31/73	0.971	0.375		-0.8			0.351563		-0.75
1	12/31/72 12/31/71	0.02 0.141	0.214 0.173		-1.8	12/31/72	0.02	0.214		-1.8
	12/31/70	0.052	0.173		-1.4	12/31/71 12/31/70	0.141 0.052	0.173 0.45		-1.4
	12/31/69	0.04	0.256			12/31/69	0.032	0.45		Ì
	12/31/68	0.023	0.134			12/31/68	0.023	0.134		}
	12/31/67	0.011	0.327			12/31/67	0.011	0.327		
	12/31/66	0.104	0.111			12/31/66	0.104	0.111		
	12/31/65	0.044	0.694			12/31/65	0.044	0.694		
1	12/31/64	0.023	0.196			12/31/64	0.023	0.196		
	12/31/63	0.023	0.034			12/31/63	0.023	0.034		
	12/31/62	0.003	0.197			12/31/62	0.003	0.197		
	12/31/61 12/31/60	0.009 0.007	0.184 0.129			12/31/61 12/31/60	0.009	0.184		
	12/31/59	0.007	0.129			12/31/50	0.007 0.003	0.129 0.048		
	12/31/58	0.000	0.025			12/31/58	0.003	0.025		- 1
	12/31/57	0.011	0.073	•		12/31/57	0.011	0.023		}
	12/31/56	0.011	0.072			12/31/56	0.011	0.072		
	12/31/55	0.012	0.095			12/31/55	0.012	0.095		
	12/31/54	0.001	0.299			12/31/54	0.001	0.299		
	12/31/53	0.044	0.089			12/31/53	0.044	0.089		
}	12/31/52	0.003	0.024			12/31/52	0.003	0.024		
1	12/31/51 12/31/50	0.003 0.006	0.017 0.231			12/31/51	0.003	0.017		
<u> </u>	12/31/30	0.006	0.231			12/31/50 12/31/49	0.006 0.006	0.231 0.022		1
	12/31/48	0.000	U.ULL			12/31/49	0.006	0.022		}
	12/31/47	0.007				12/31/47	0.007			
	12/31/46	0.001				12/31/46	0.001			ŀ
	12/31/45	0.006				12/31/45	0.006			
	12/31/44	0.002				12/31/44	0.002			
	12/31/43	0.012				12/31/43	0.012	•		
	12/31/42	0.017				12/31/42	0.017			
}	12/31/41	0.03				12/31/41	0.03			
	12/31/40 12/31/39	0.144 0.161				12/31/40	0.144			
	12/31/38	0.062				12/31/39 12/31/38	0.161 0.062			1
	12/31/37	0.033				12/31/37	0.033			
	12/31/36	0.028				12/31/36	0.028			
	12/31/35	0.013				12/31/35	0.013			j
	12/31/34	0.002				12/31/34	0.002			

Figure 49

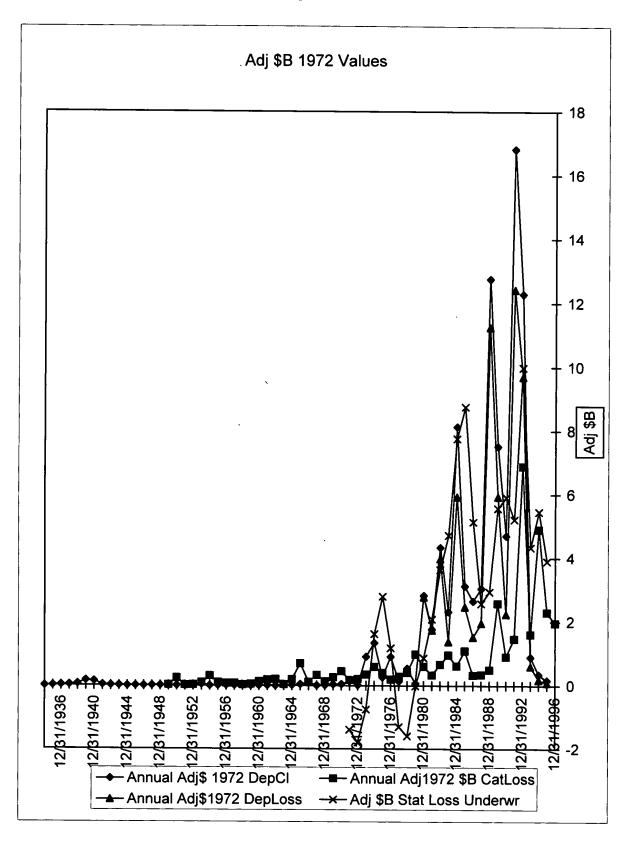


Figure 51

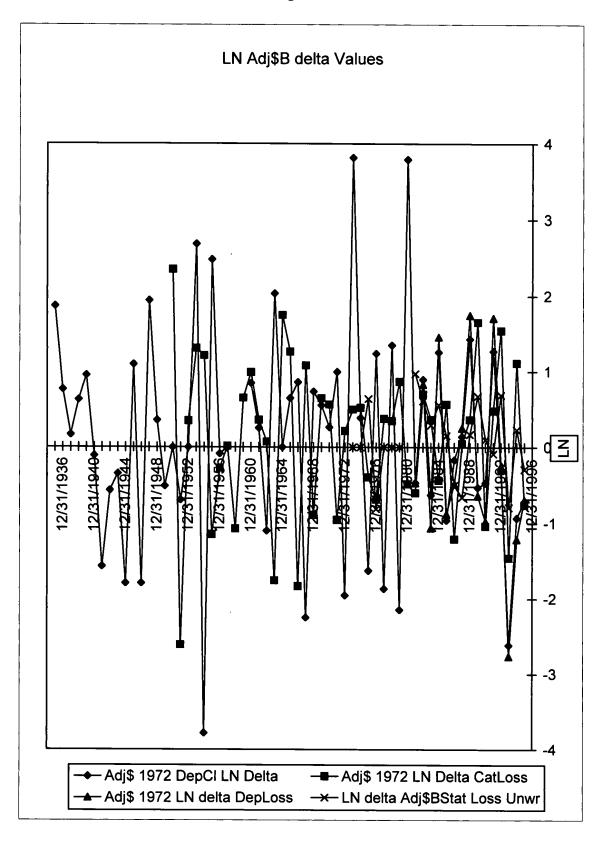


Figure 60

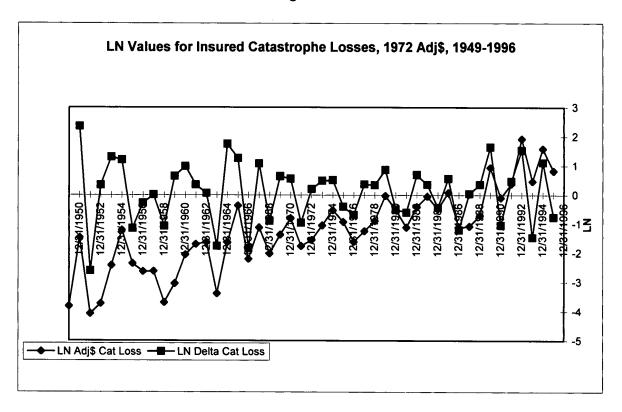


Figure 61

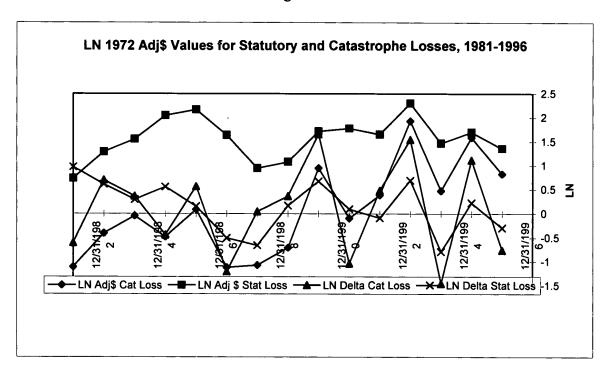


Figure 85

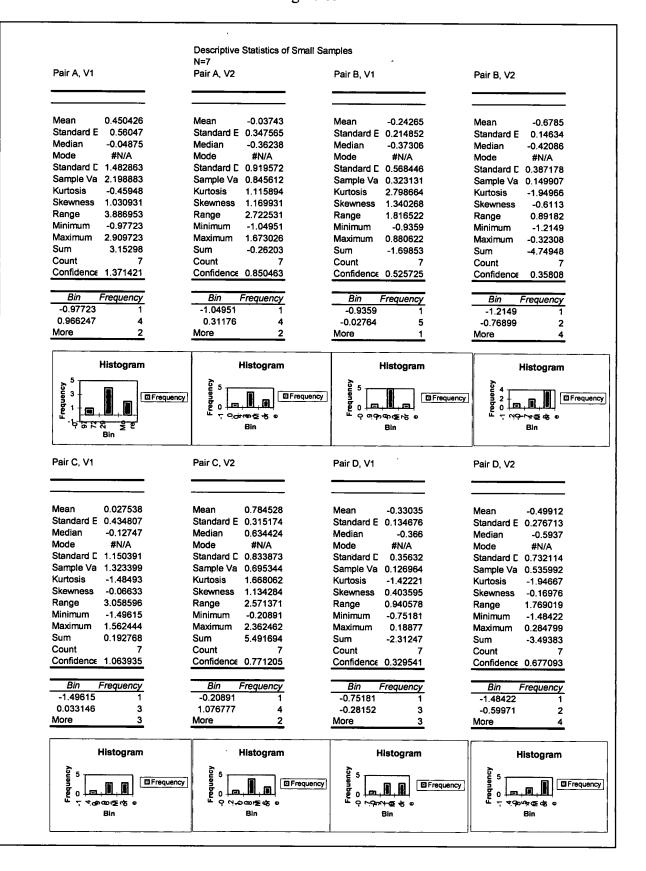


Figure 86

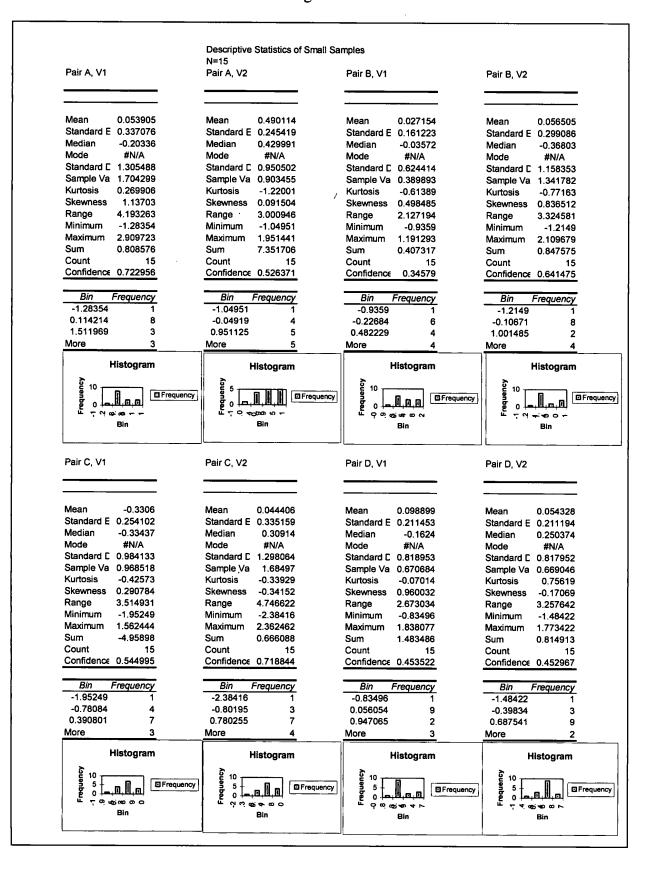
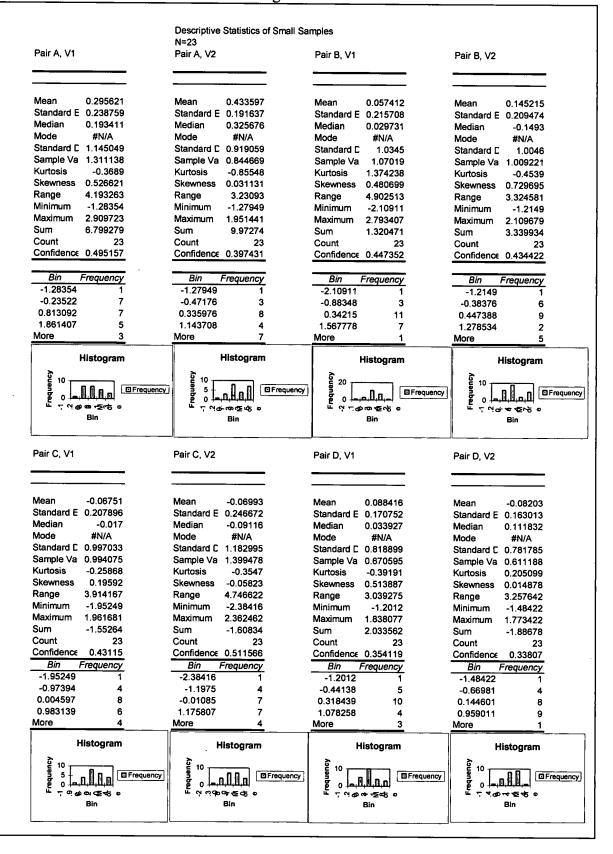


Figure 87



Temporary disable feature on memory and/or graphics, internal or as outside device, for tests

this enables the calculators to be used in test environments without further ado or loss by having temporary disable feature, memory is not deleted, but is non-functional for tests disable memory and/or graphics functions for a time period, so the calculator can be used: an internal disable feature with timed duration, using the processor's clock to count time or by central storage, memory loading, device, with storage space per calculator in group.

Figure 96

Short coded demos in on-board memory of interesting usage, topics, subjects and formulae

it's always fun for an electronic device to have simple programs, showcasing capabilities it's always good for dedicated devices to stimulate interest and learning in their subject the depth of features available in such calculators often remain hidden from casual use: demos on topics, functions and formulas in memory, wherein elaboration in user manual the user manual is organized, conceived and focused on capabilities, usage, applications examples: reference items, formulae, even graphical art generations, sample, "Insect": graph in polar: $r1 = 5\cos(2\Pi)$; $r2 = 2+2\cos(2\theta)$; $r3 = 5-2\tan(5\theta)$; $r4 = 4+4\sin(2+2\theta)$. add brief elaboration and context to educate, to inform; see also Reference Resources.

Figure 97

Resident resource compendia, RAM/ROM sets, providing coded functions and items on-board

not much on-board memory need be taken up by assorted demos, being fixed-coded items by executing demos on user command, stored graphics, results or images are not required add required list, group or function for the variety of subject expositions ala encyclopedia: target assemblage of reference compendia to varied educational levels of math and science high school version supports teaching of geometry, algebra, probability, calculus, sciences elementary to college versions help educate; scaleable to lower end units, and useable in all; make advanced specialized resources per industry, as modules loaded to RAM or installed per electrical, mechanical, environmental, financial engineering; math, physics, astronomy such items include today's methods, theorems, formulae, procedures, pre-coded functions compendia add pivotal resources: references, equations, algorithms, processes, programs.

Figure 98

professional standard industry-specific software, pre-loaded or accessible through interface

develop the reference resources along with subject functions coded to existent calculators arm a portion of calculator memory with compendium of equations, conversions, etc. some to full pre-loading, or as modules by industry fields, with downloading to RAM

Figure 99

value-added software is packaged as desirable assets for different operational specialties

Calculator has application archives, of science, math, engineering, focus on user-friendly proper subject archives arranged, to be categorically supplemented by newly coded items new archives are value-added property to integrate, install, or avail, by cable, line or net all software can be pre-loaded (opt. delete), be availed separately, or transmitted on-line provide additional access and memory capacity, i.e. RAM/ROM cards, ext/int drive/storage technology path of calculator unit on improved digital interfaces, bus, PCMCIA, memory.

	Resident Financia	al Equations and A	Algorithms coded f	for use in Equation (iterative	e) Solver, include:
1	AI CorpB	AI TB	Annuity	Bond Equiv Yield	Bin 1, Bin2, Bin 3
	Binomial	BS	Bond	BonK, BonV	Brown
	CBT	CLT	Comp	Con, Conadj, Condp	Convexity
	DeltaP, dP	dPdY	DurMod	DurMc	DV01
	FFOTD	Forward	FX	Hedge, HR	MDS
	Min1,Min2,Min3	Mortgage	MPC	Muni	OAS3 (example)
ł	OCF	PAY, PAY1	PR, PRBond	PRCalB, PRMunat	PRO `
1	PROMOD	PROPC	PTIC	PV	SPC
	Spot	Swap	FXSwap	Tbill1, TB2,	ТВТ
	TDCap	V	Var	W	BoxMuller

Bernoulli	optionbond	Borel-Cantelli	for display to screen Boundary	Brownian
Option	optionlog	CAPM	Chebychev	Correlation
CoVar	Credit	cut-off	distfunc	E(N)
EQU	EX	Floater	FOCF	GenFunc
GcS	lattice	Inde	Intre	Ito
Lambda	lease	martingale	minrisk	mpr
partition	PCP	Poisson	Portf	RandomW
replication	riskadverse	SPC	strong	theorfut
tokens	tree	utility	weak	weight

Other Re	ference Resource	Sources for I	Financial Matter,	Data, Equations and References, include:
		Newspapers		Real-time digitized data providers

Resident Processing, Reference Resource Items and Programmed Functions, include:

clock, date, calendar, default value present time/date

equation solver function and simultaneous equation solver function

intervals between dates, coupons, valuation, exercise, expiration

day-count conventions, instrument standards, conversions

fixed-income general valuations (annuity, mortgage, lease, bond, rates and yields)

fixed-income advanced valuations (variable cash-flows, inverse, MBS, sinking, optionality)

fixed-income derivative valuations (options, futures basis, hedge ratios, swaps, FX dP/dY)

fixed-income and derivative sensitivities (duration, convexity, delta, gamma, theta, dtheta)

fixed-income yield curve building (spot, risk-free short rates and forward curves)

accounting standards, (GAAP, statutory, derivatives, credit quality, risk-adjusted capital)

financial statement and performance ratios, operating ratios of financial criterion

credit and ratings grade conventions, calculating ratings and spread approximations

insurance ratios, pricing, quantitative methods

reinsurance forms and pricing of excess of loss, facultative, treaty varieties

actuarial mathematics and sciences, loss distributions, contingencies, survival models

standard normal and lognormal random number generation, selectable N, descriptive statistics of sample

simulations by lattice, brownian motion, random sequence generation, interpolation

portfolio management of VaR, performance analytic measures

direct approximations by derivation, linear algebra, symbolic, integration, interpolation

mapping to charts, display multiple list and graphical display (to 3D)

one, two and more variable statistics and multi-factor regression

time series and artificial intelligence data mining, normalization procedures

inferential and descriptive statistics, probability distributions

real-time and formatted data loading and serial, IRDA and TCP/IP

stored column formulas, spreadsheet capability, data set manipulation

split screen, display size minimum pixels 128x64, 8x21 display characters

trace, overlay (or by split screen) and combine scatter plots, histograms, interpolations, results.